

# **FINS STUDY AID**

**MECH-420 Heat Transfer**  
**Dr. K. J. Berry**



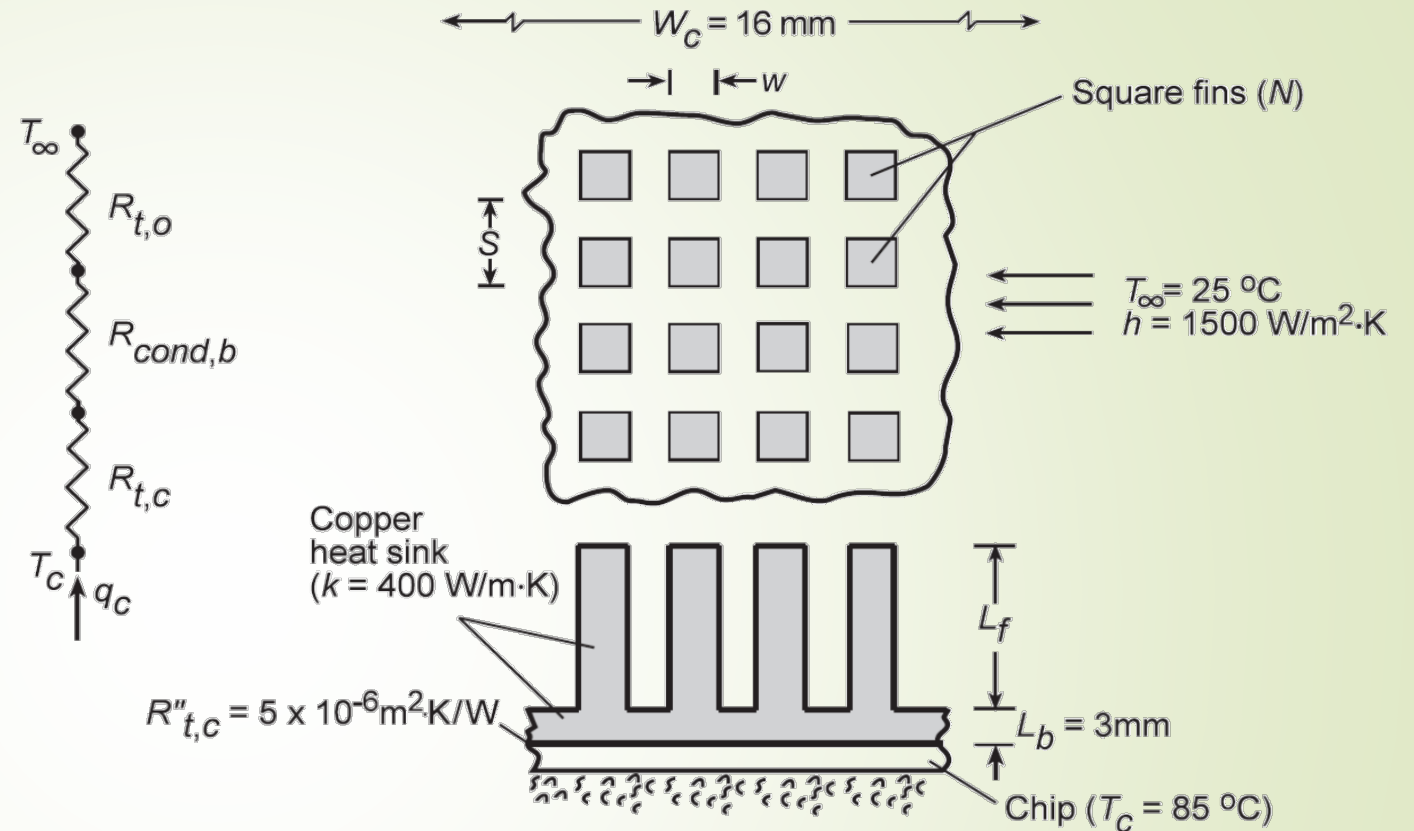
# FINS: EXTENDED SURFACES (CLICK)

MECH-420 Heat Transfer  
Section 3.6



Square Copper Heat Sink Fins attached to electronic chip.

Determine # fins required for desired power dissipation of 200W



# Determine FIN Base Temperature Due to Contact Resistance

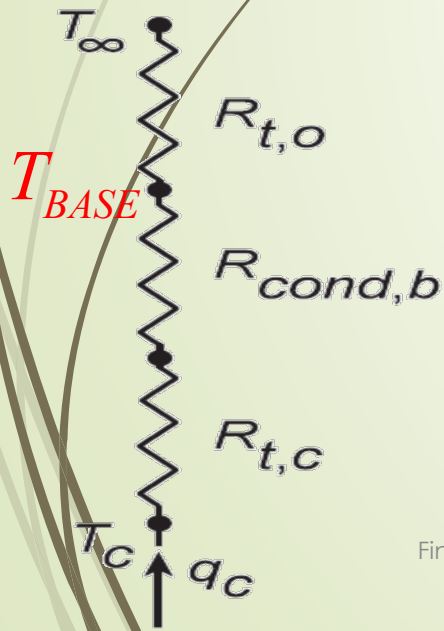
4

$$k = 400 \frac{W}{m-K}$$

$$L_b = 3mm$$

$$L_f = 6mm$$

$$W_c = 16mm$$



$$q = 200W = \frac{(T_c - T_{base}) K}{\frac{R_{tc}'' \left[ \frac{m_2 - K}{W} \right]}{W_c^2 [m^2]} + \frac{L}{kA}}$$

$W_c \rightarrow WIDTH$

$$T_{base} = T_c - q[W] \cdot \left( R_{tc}'' \frac{m_2 - K}{W} \left[ \frac{1}{W_c^2 m^2} \right] + \frac{L_b}{kA} \frac{m}{W - m^2} \right) \frac{1}{m - K}$$

$$= 85C - \left[ 200W \cdot \left( \frac{5 \times 10^{-6}}{\left( \frac{16}{1000} \right)^2} + \frac{3 / 1000}{400 \frac{W}{m - K} \cdot \left( \frac{16}{1000} \right)^2} \right) \right]$$

$$= 85C - 200(0.01953 + 0.0293)$$

$$= 75.2C$$

# Find Heat Transfer for Single Fin (Case A)

5

$$k = 400 \frac{W}{m^2 \cdot K}, h = 1500 \frac{W}{m \cdot K}, w = 0.25 \text{ mm}, T_{\infty} = 25 \text{ C}, T_b = 75.2 \text{ C}$$

$$P = 4w = 0.001 \text{ m}, L_f = 6 \text{ mm}$$

$$A_c = w^2 = 6.25 \text{ E} - 08 \text{ m}^2$$

$$m = \sqrt{\frac{hP}{kA_c}} = \sqrt{\frac{1500 \frac{W}{m \cdot K} \cdot 0.001 \text{ m}}{400 \frac{W}{m^2 \cdot K} \cdot 6.25 \text{ E} - 08 \text{ m}^2}} = 245 \frac{1}{\text{meters}}$$

$$M = \sqrt{hPkA_c} \theta_b = 0.006124 \theta_b = 0.3074 \text{ W}$$

$$h / mk = 0.0153$$

$$mL = 1.47, \sinh(mL) = 2.06, \cosh(mL) = 2.29$$

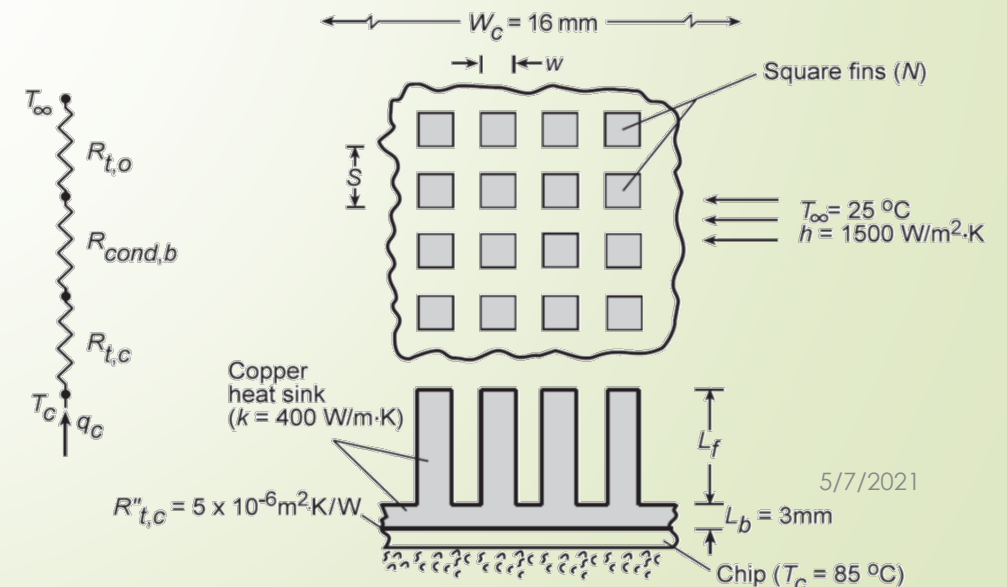
$$q_f = M \frac{\sinh mL + (h / mk) \cosh mL}{\cosh mL + (h / mk) \sinh mL}$$

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$$h / mk = 0.0153$$

$$mL = 1.47, \sinh(mL) = 2.06, \cosh(mL) = 2.29$$

$$q_f = 0.3074 \frac{2.06 + 0.153 \cdot 2.29}{2.29 + 0.153 \cdot 2.06} = 0.2844 \text{ W}$$



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# Fin Efficiency

6

$$\eta_{fin} = \frac{\text{Fin Heat Transfer Rate}}{\text{MAX HEAT TRANSFER POSSIBLE}} = \frac{q_{fin}}{q_{max}} = \frac{q_{fin}}{hA_{FIN\ TOTAL}\theta_b} \rightarrow 0-1$$

$A_{FIN\ TOTAL}$  = TOTAL FIN AREA EXPOSED TO FLUID

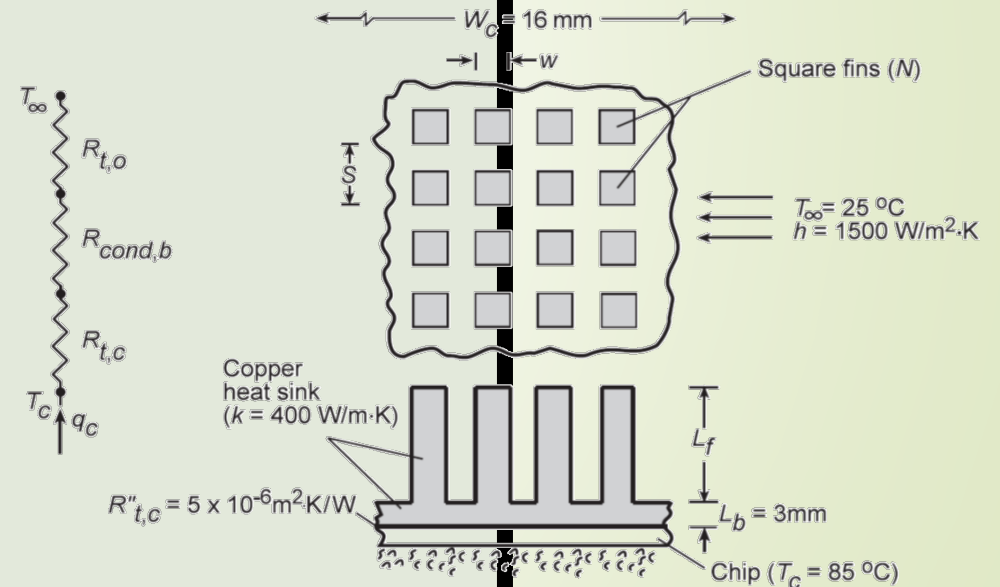
$$\theta_b = T_b - T_\infty$$

$$P = 4w = 0.001m, L_f = 6mm$$

$$A_{fin} = P \cdot L_{fin} + w^2 = 0.001m \cdot 0.006m = 6.0625 \times 10^{-6} m^2$$

$$q_{max} = 1500 \frac{W}{m^2 \cdot K} 6 \times 10^{-6} m^2 (75.2 - 25) = 0.4518 W$$

$$\eta_{fin} = \frac{0.2844}{0.4518} = 0.6295 (63\%)$$



# MAX HEAT TRANSFER

7

$$q_{\max} = 1500 \frac{W}{m^2 \cdot K} 6 \times 10^{-6} m^2 (75.2 - 25) = 0.4518 W$$

$$\eta_{fin} = \frac{0.2844}{0.4518} = 0.6295 (63\%)$$

$$q_{TOTAL} [W] = N \eta_{fin} q_{MAXIMUM} + h A_0 \theta_b \rightarrow \text{FIN BASE AREA}$$

$$A_0 = W^2 - w^2 N \rightarrow$$

$$w = 0.25 \text{ mm}, W = 16 \text{ mm}$$

$$q_{TOTAL} [W] = N \eta_{fin} q_{MAXIMUM} + h \theta_b (W^2 - w^2 N)$$

$$= N (\eta_{fin} q_{MAXIMUM} - h \theta_b w^2) + h \theta_b W^2$$

$$N = \frac{q_{TOTAL} [W] - h \theta_b W^2}{\eta_{fin} q_{MAXIMUM} - h \theta_b w^2}$$

$$= \frac{200 - 1500 * 50.2 * 0.016^2}{0.63 * 0.4518 - 1500 * 50.2 * 0.00025^2}$$

≈ 634 Fins (26x26 Fin Array @ Spacing 0.50mm/fin)

= 13x13 mm<sup>2</sup> Heat Sink

